

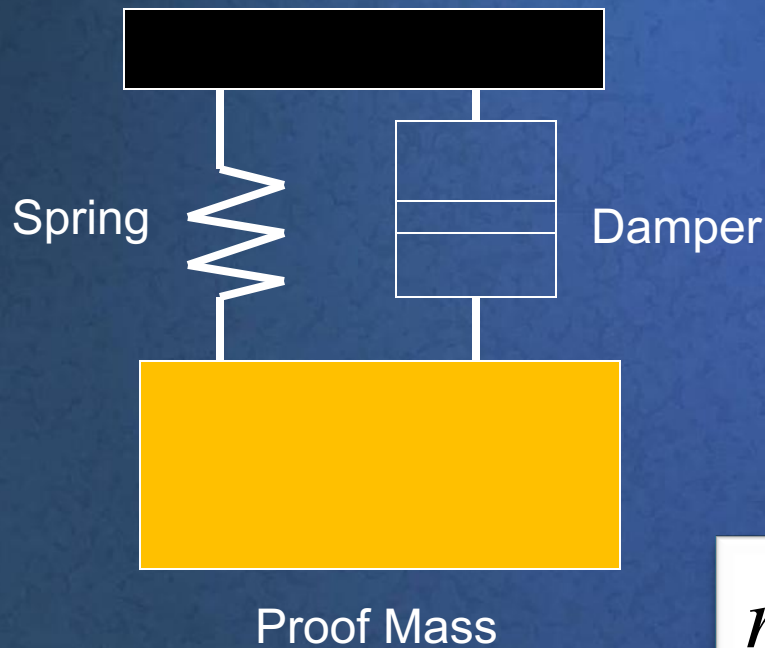
Accelerometers on Flexible Substrates

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Physical Structure of an Accelerometer

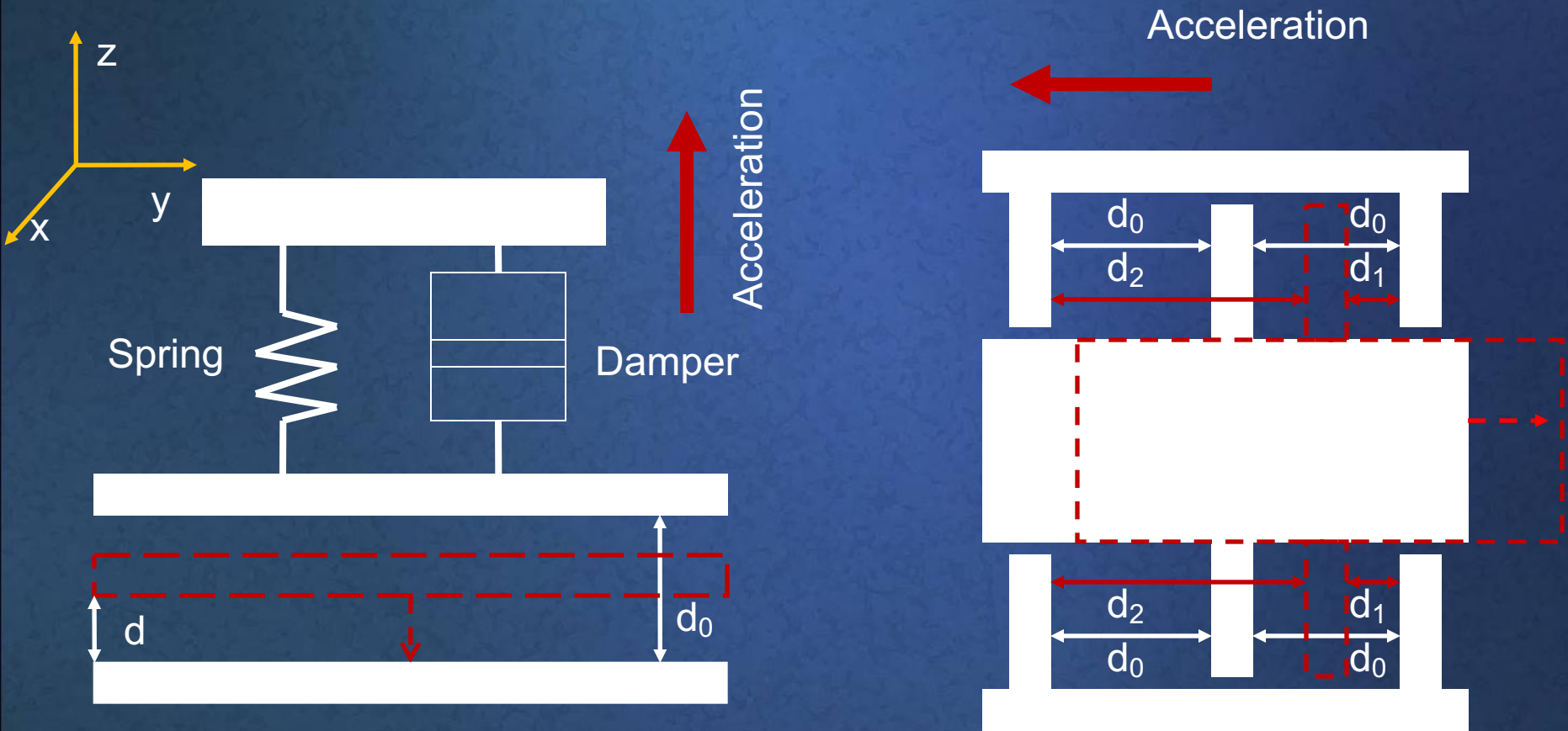


The structure of an accelerometer is formed by proof mass, damper and a spring. Whenever there is an acceleration, the proof mass moves which is opposed by the spring and the damper.

$$m \ddot{x} + b_m \dot{x} + k_m x = F_x(t)$$

•J. W. Gardner, V. K. Varadan and O. O. Awadelkarim, "Microsensors, MEMS and Smart Devices"
, John Wiley and Sons, 2005

Basic Principle of Capacitive Accelerometer

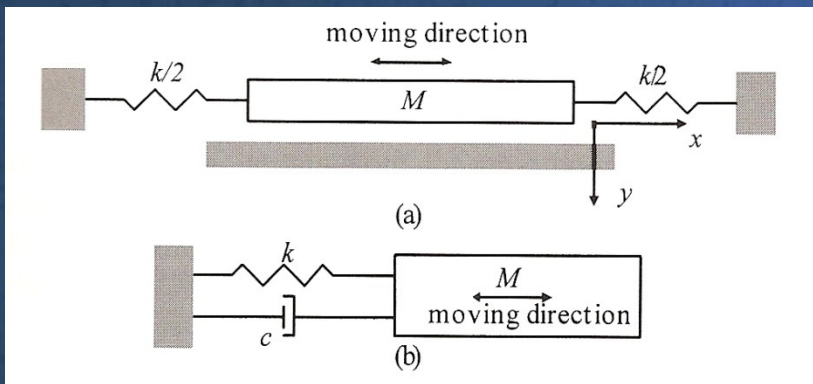


Accelerometer is based on parallel plate capacitance between a fixed plate and a movable plate connected to a spring. Acceleration is determined by the change in capacitance.

Damping Force

Damping: Dissipative forces such as friction, viscosity which take energy from the system and restrict its movement,

Slide Film Air Damping



$$\delta = \sqrt{2\mu / \rho\omega}$$

Effective decay distance

Low ω , $\delta \gg d$ (Couette Flow)

δ comparable to d (Stokes Flow)

Navier-Stokes Equation

$$\rho \left[\frac{\partial \vec{v}}{\partial t} + (\vec{v} \cdot \nabla) \vec{v} \right] = \vec{F} - \nabla p + \mu \nabla^2 \vec{v}$$

$$\vec{v} = u \vec{i} + v \vec{j} + w \vec{k}$$

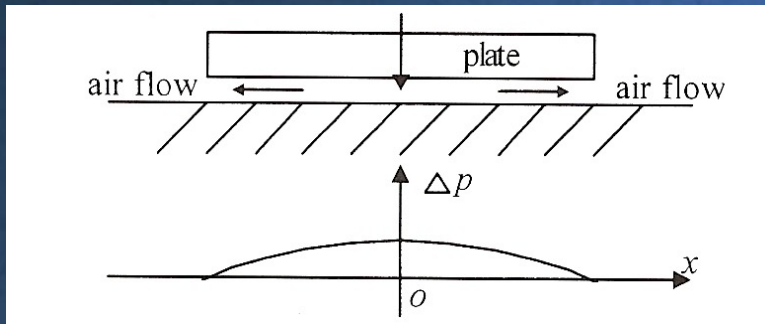
$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} = \frac{\mu}{\rho} \frac{\partial^2 u}{\partial z^2}$$

Movement in x-direction only

$$u(t) = a_0 \omega \cos \omega t = u_0 \cos \omega t$$

Damping Force

Squeeze Film Air Damping



$$\omega_0 = \sqrt{\frac{k}{m}}$$

Free vibration frequency

$$\omega_c = \frac{\pi^2 h_0^2 p_a}{12 \mu w^2}$$

Cutoff frequency (elastic force equals damping force)

When $\omega_0 \ll \omega_c$

- Gas film is assumed to be incompressible.
- Coefficient of damping force is assumed constant.
- Squeeze action is slow and there is time for gas to leak.

$$\xi = c_{d0} / 2m\omega_0$$

$\xi < 1 \rightarrow$ under damped (continues to oscillate at natural frequency)

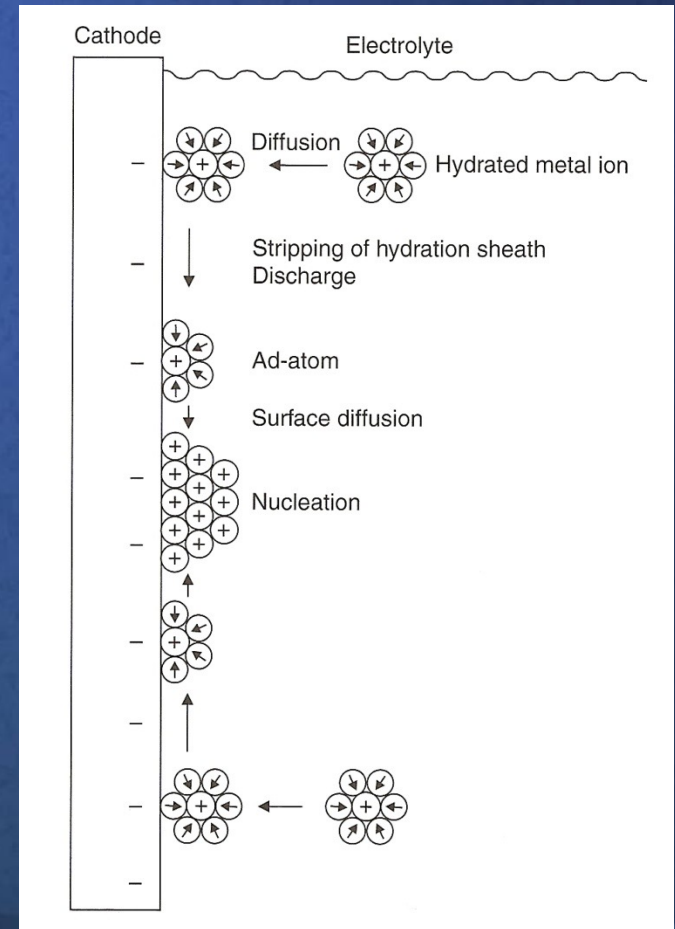
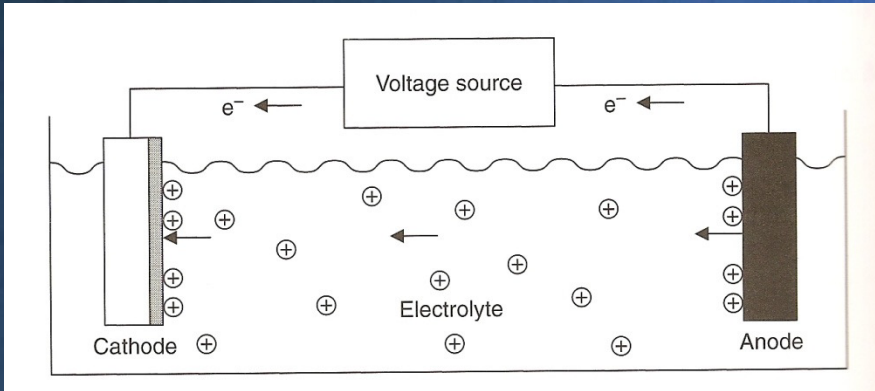
$\xi = 1 \rightarrow$ critically damped (comes to rest instantaneously)

$\xi > 1 \rightarrow$ over damped (takes longer to come to rest)

• M. Bao, "Analysis and Design Principles of MEMS Devices", Elsevier, 2005

• M. Bao and H. Yang, "Squeeze Film Air Damping in MEMS", Sensors and Actuators A, vol. 136, pp. 3-27, 2007

Electroplating

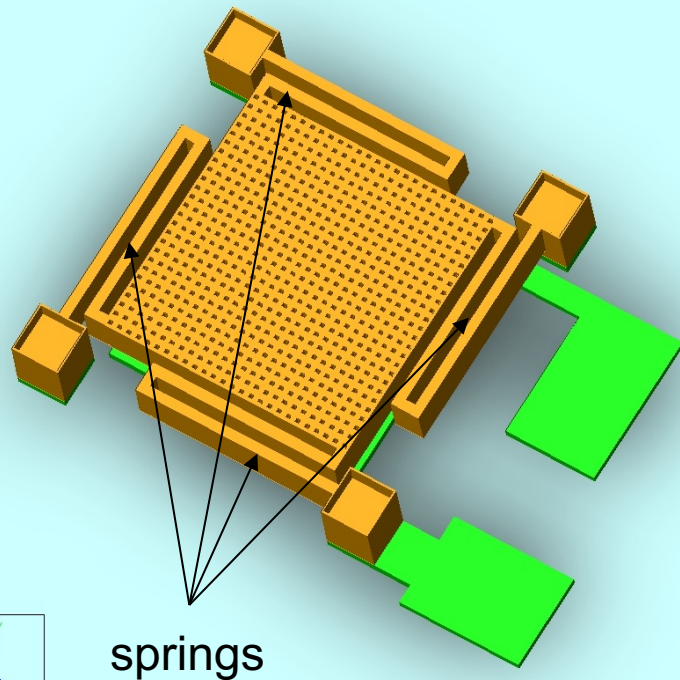


- Diffusion to cathode
- Metal ion discharge at cathode
- Nucleation through surface diffusion
- Fusion of nuclei to form a continuous film

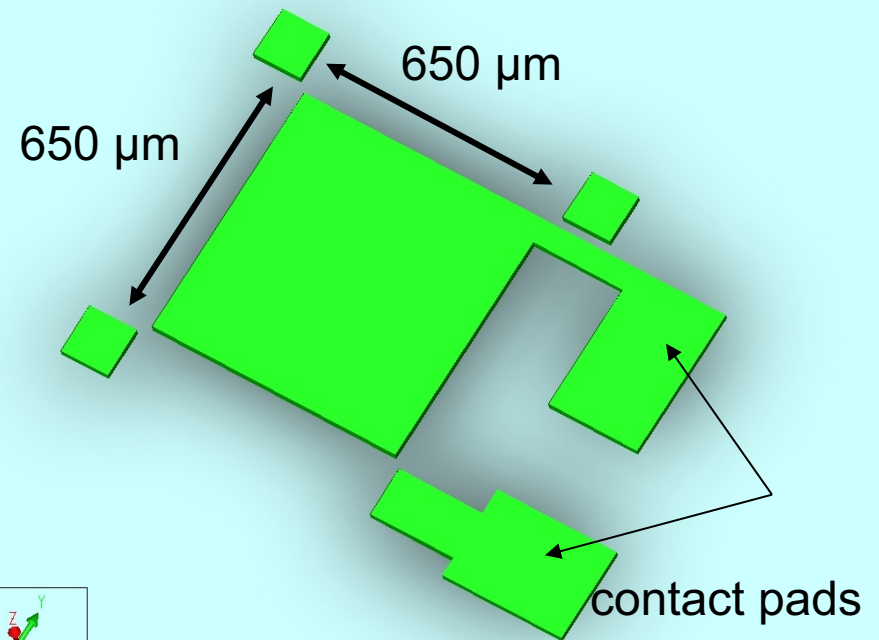
Accelerometer Design

Device 1

WHOLE STRUCTURE



BOTTOM ELECTRODES



Accelerometer Design

		Z-AXIS
Spring Constant (N/m)		10.118 (7.998)*
Damping Ratio	-40 °F	0.550
	60 °F	0.658
	160 °F	0.753
Frequency (kHz)		25.297
Rest capacitance (pF)		1.894
ΔC (fF/g)		18.08
Mass (kg)		$1.581 \cdot 10^{-8}$

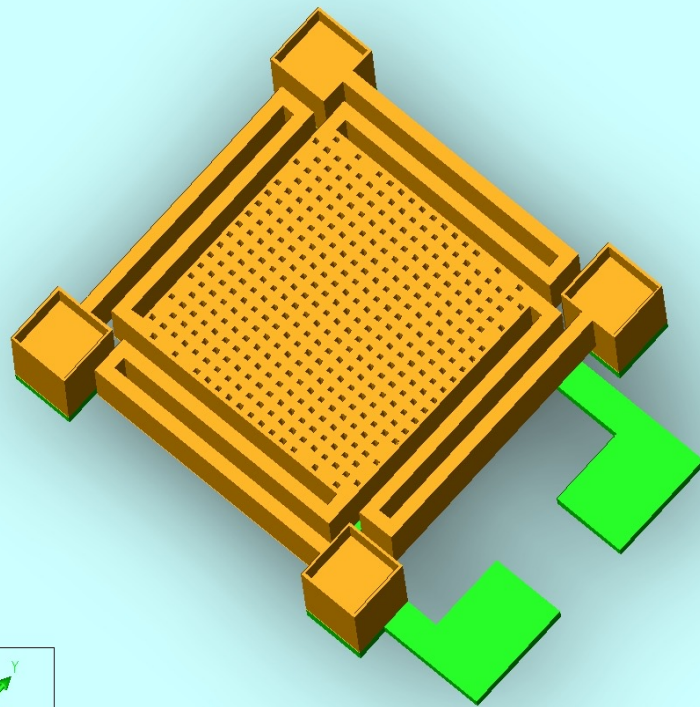
Device 1 Results

* Calculated from displacement

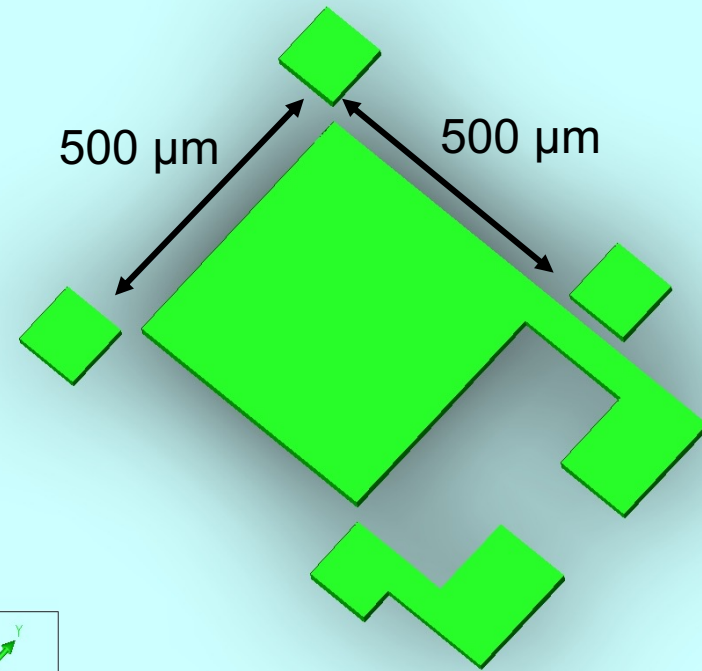
Accelerometer Design

Device 2

WHOLE STRUCTURE



BOTTOM ELECTRODES



Accelerometer Design

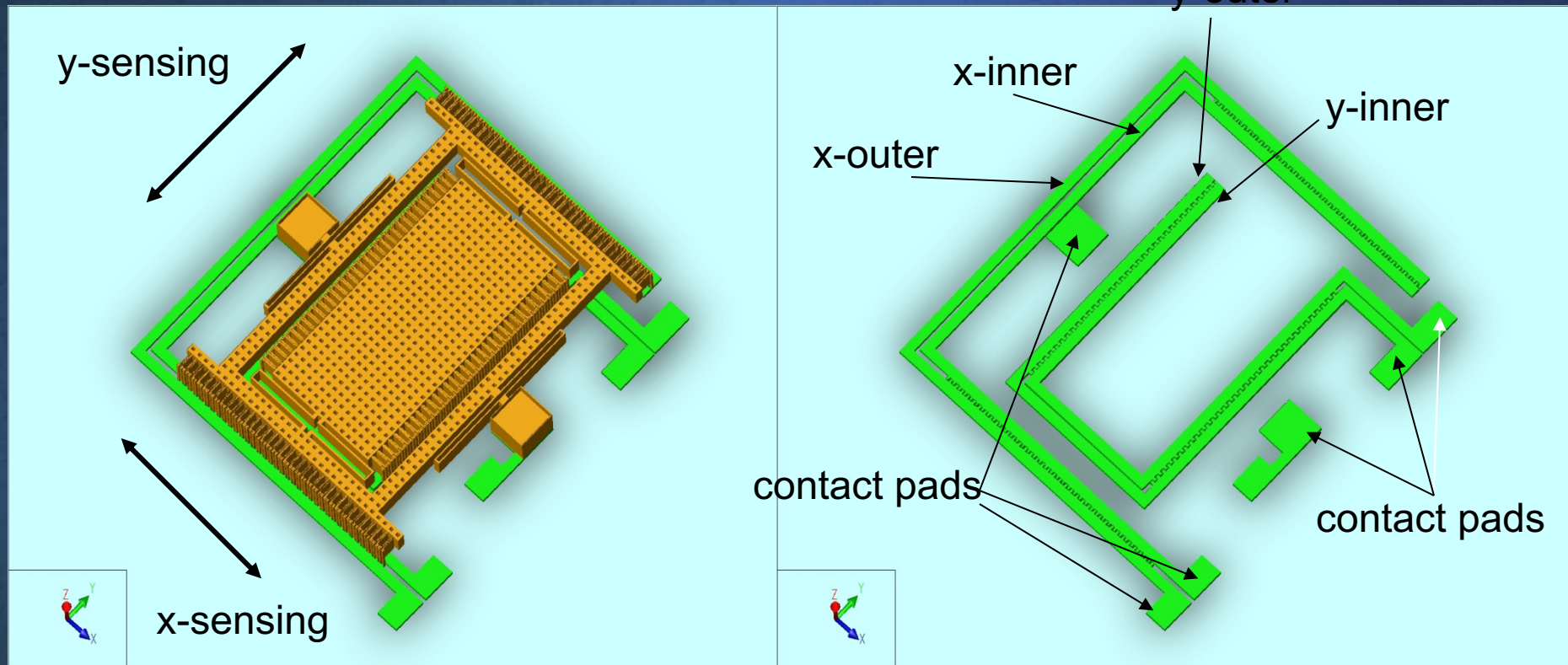
		Z-AXIS
Spring Constant (N/m)		10.118 (7.488)*
Damping Ratio	-40 °F	0.553
	60 °F	0.661
	160 °F	0.756
Frequency (kHz)		32.188
Rest capacitance (pF)		1.125
ΔC (fF/g)		6.648
Mass (kg)		$9.766 \cdot 10^{-9}$

Device 2 Results

* Calculated from displacement

Accelerometer Design

Device 3 X AND Y SENSING ON THE SAME STRUCTURE



Dimensions: $1605\ \mu\text{m} \times 1281\ \mu\text{m}$ for x-axis and $1550\ \mu\text{m} \times 910\ \mu\text{m}$ for y-axis
(INCLUDING COMB LENGTHS)

Number of movable combs: 72 for x-axis and 68 for y-axis

Effective comb length: $71\ \mu\text{m}$ for x-axis and $75\ \mu\text{m}$ for y-axis

Accelerometer Design

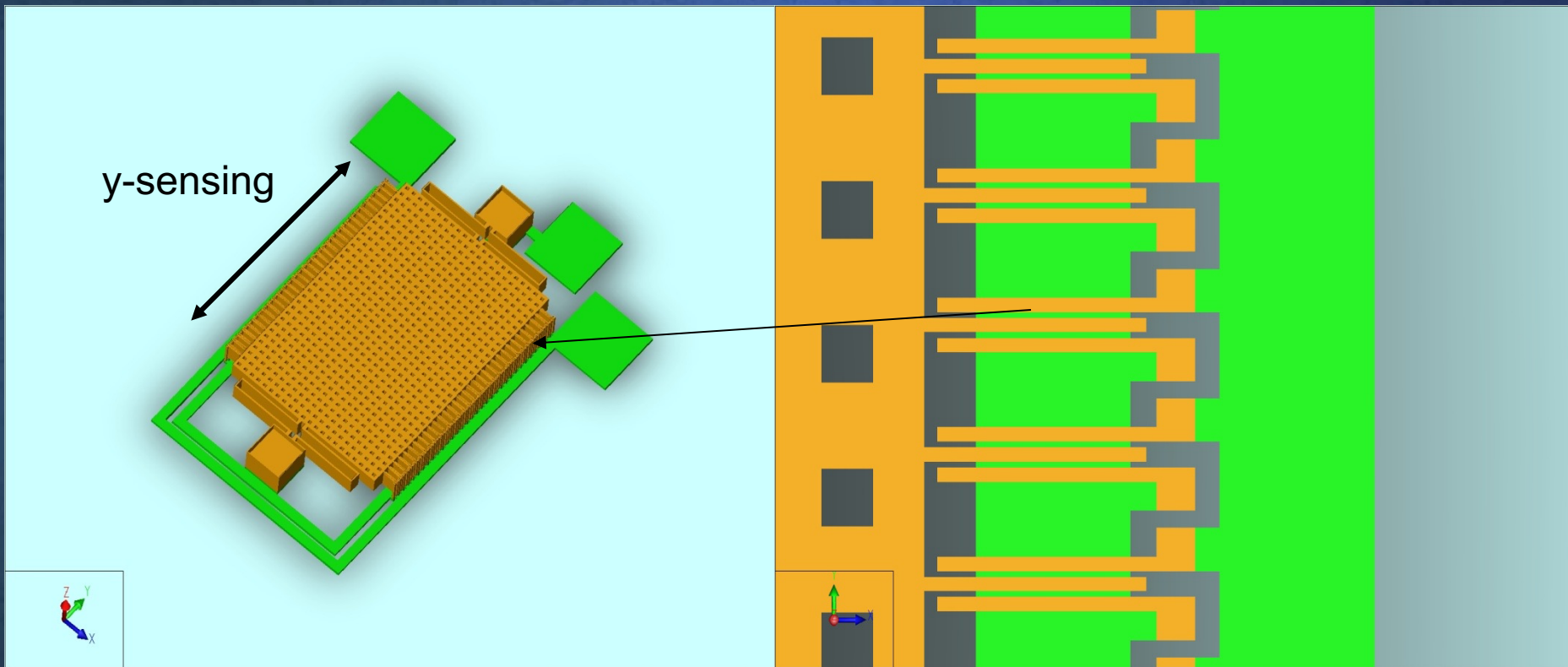
		X AXIS	Y AXIS
Spring Constant (N/m)		12.351*	24.794*
Damping Ratio	-40 °F	0.553	0.545
	60 °F	0.661	0.651
	160 °F	0.756	0.745
Frequency (kHz)		13.086	23.549
Rest capacitance (pF)	inner	0.332	0.532
	outer	0.199	0.732
ΔC (fF/g)	inner	3.808	0.975
	outer	3.635	1.160
Mass (kg)		$7.213 \cdot 10^{-8}$	$4.471 \cdot 10^{-8}$

Device 3 Results

* Calculated from displacement

Accelerometer Design

Device 4 SAME TWO STRUCTURES ORTHOGONAL WITH RESPECT TO EACH OTHER TO SENSE BOTH X AND Y AXIS



Dimensions: 1605 μm x 1281 μm (INCLUDING COMB LENGTHS)

Number of movable combs: 66

Effective comb length: 81 μm

Accelerometer Design

		X AND Y-AXIS
Spring Constant (N/m)		24.063 (24.223)*
Damping Ratio	-40 °F	0.548
	60 °F	0.655
	160 °F	0.749
Frequency (kHz)		18.799
Rest capacitance (pF)	inner	0.386
	outer	0.230
ΔC (fF/g)	inner	2.05
	outer	2.045
Mass (kg)		$6.809 \cdot 10^{-8}$

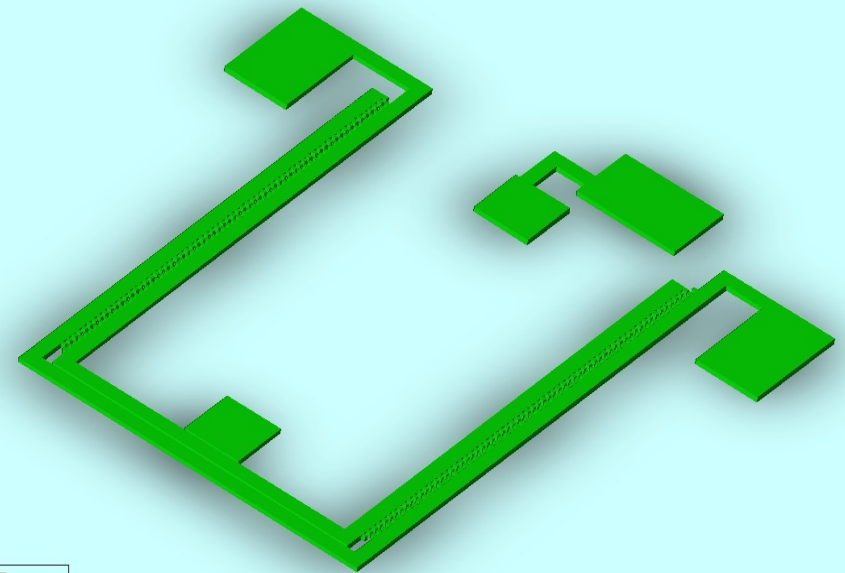
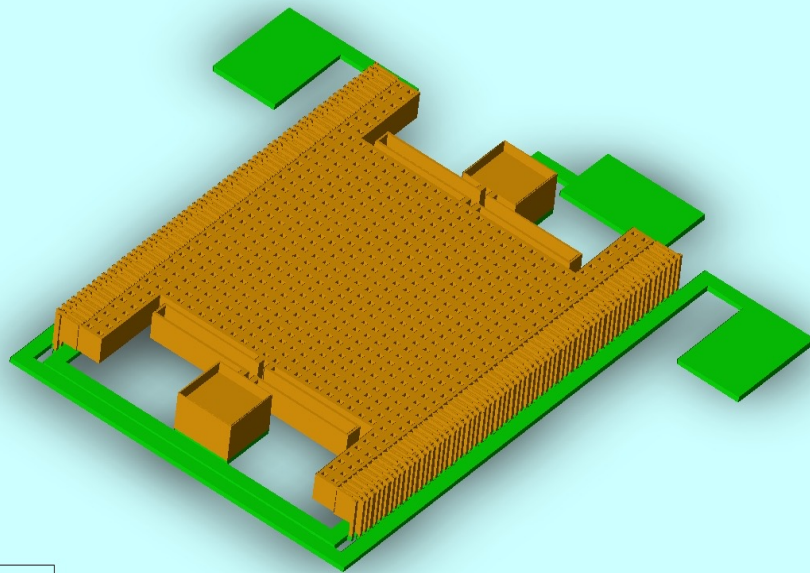
Device 4 Results

* Calculated from displacement

Accelerometer Design

Device 5

SAME TWO STRUCTURES ORTHOGONAL WITH RESPECT TO EACH OTHER TO SENSE BOTH X AND Y AXIS



Dimensions: $1900\ \mu\text{m} \times 1338\ \mu\text{m}$ (INCLUDING COMB LENGTHS)

Number of movable combs: 128

Effective comb length: $64\ \mu\text{m}$

Accelerometer Design

		X AND Y-AXIS
Spring Constant (N/m)		24.063 (24.230)*
Damping Ratio	-40 °F	0.559
	60 °F	0.668
	160 °F	0.764
Frequency (kHz)		19.846
Rest capacitance (pF)	inner	0.5573
	outer	0.3184
ΔC (fF/g)	inner	2.7
	outer	2.6
Mass (kg)		$6.109 \cdot 10^{-8}$

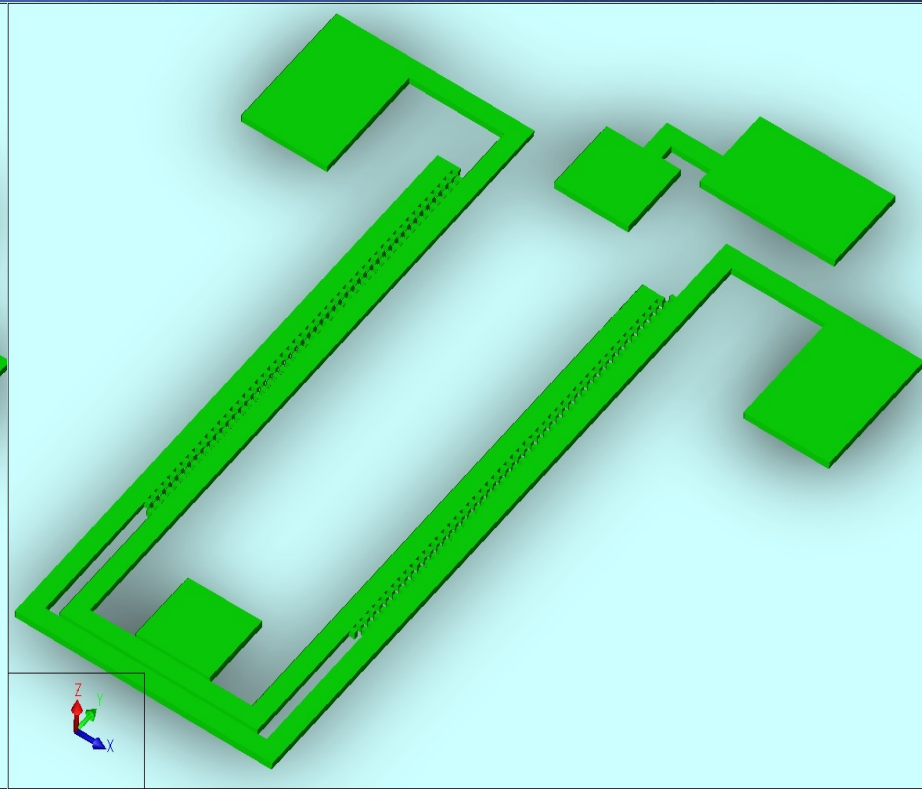
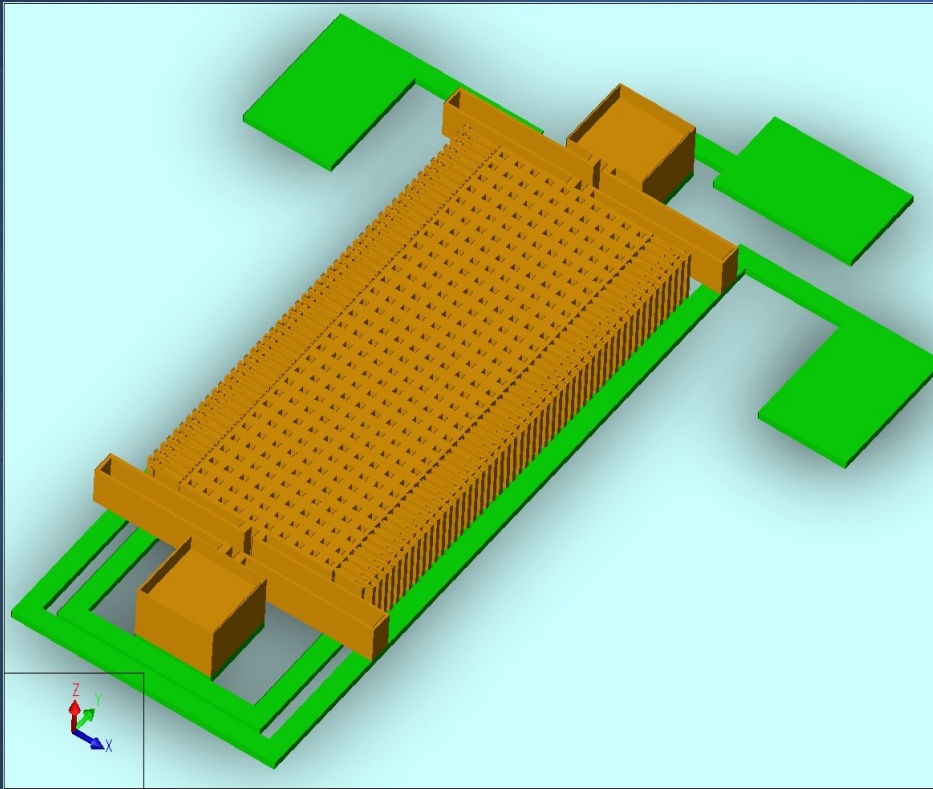
Device 5 Results

* Calculated from displacement

Accelerometer Design

Device 6

SAME TWO STRUCTURES ORTHOGONAL WITH RESPECT TO EACH OTHER TO SENSE BOTH X AND Y AXIS



Dimensions: 1500 μm x 632 μm (INCLUDING COMB LENGTHS)

Number of movable combs: 100

Effective comb length: 61 μm

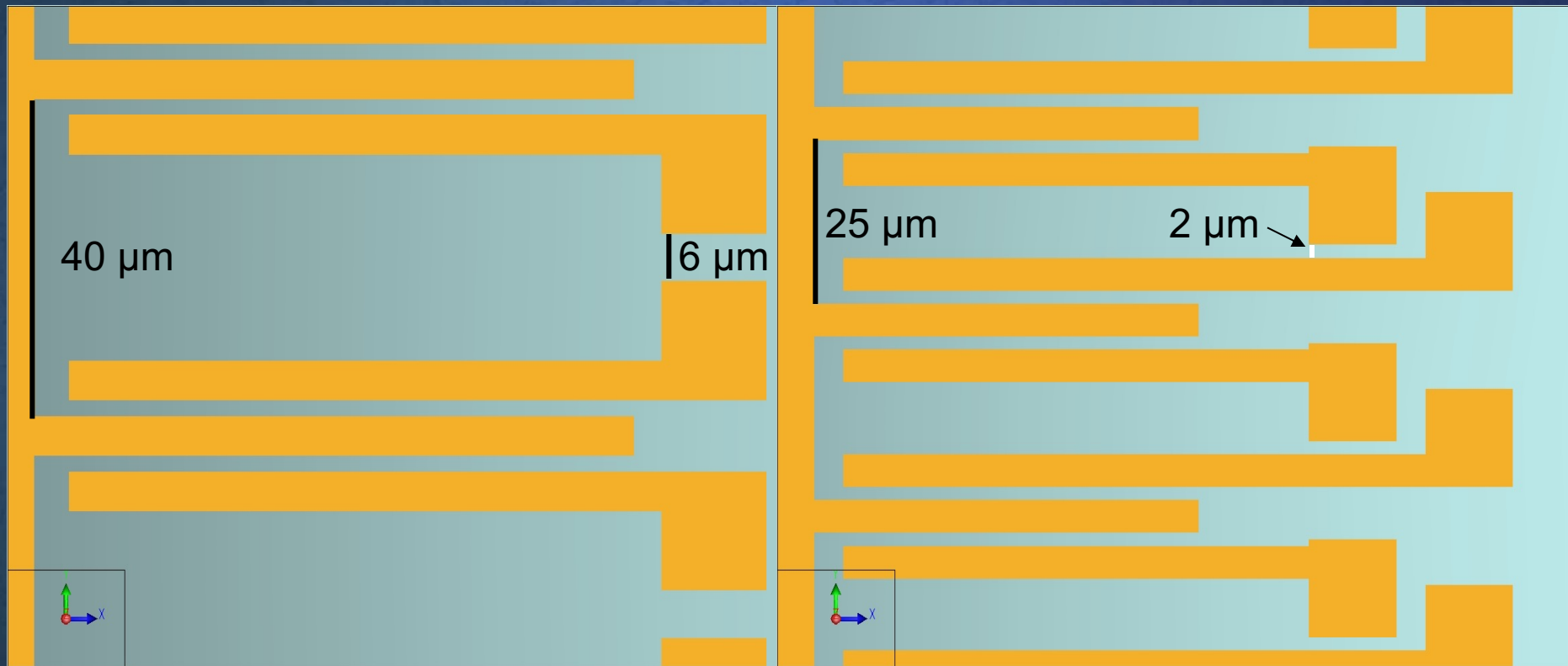
Accelerometer Design

		X AND Y-AXIS
Spring Constant (N/m)		24.063 (23.723)*
Damping Ratio	-40 °F	0.543
	60 °F	0.649
	160 °F	0.742
Frequency (kHz)		28.541
Rest capacitance (pF)	inner	0.447
	outer	0.276
ΔC (fF/g)	inner	1.016
	outer	1.011
Mass (kg)		$2.954 \cdot 10^{-8}$

Device 6 Results

* Calculated from displacement

Accelerometer Design

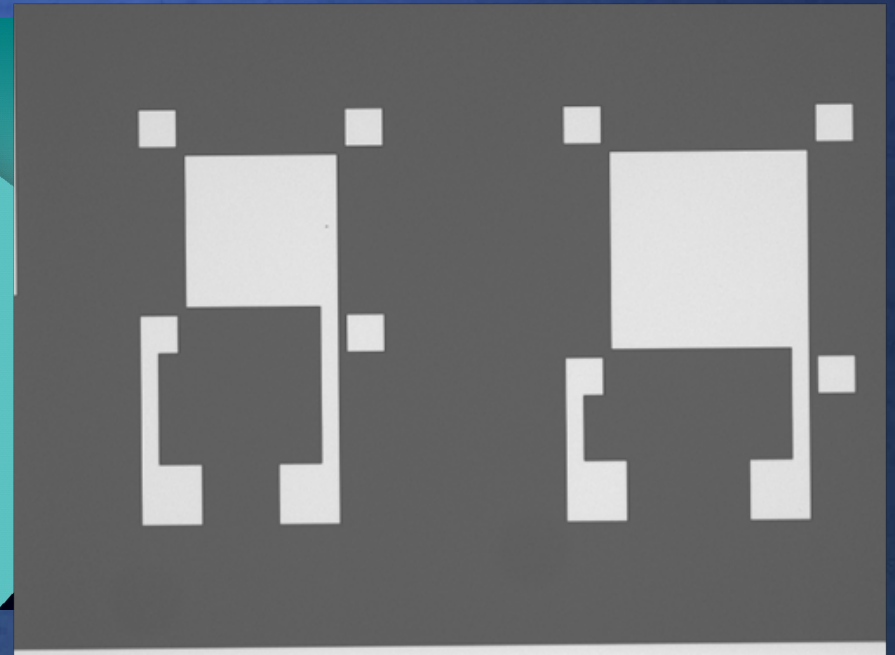
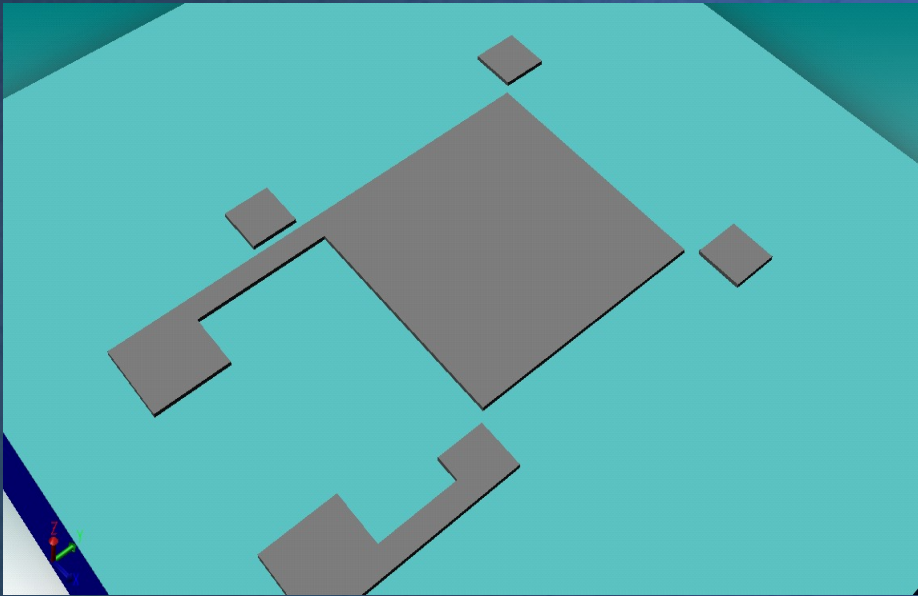


Devices 3 and 4

Devices 5 and 6

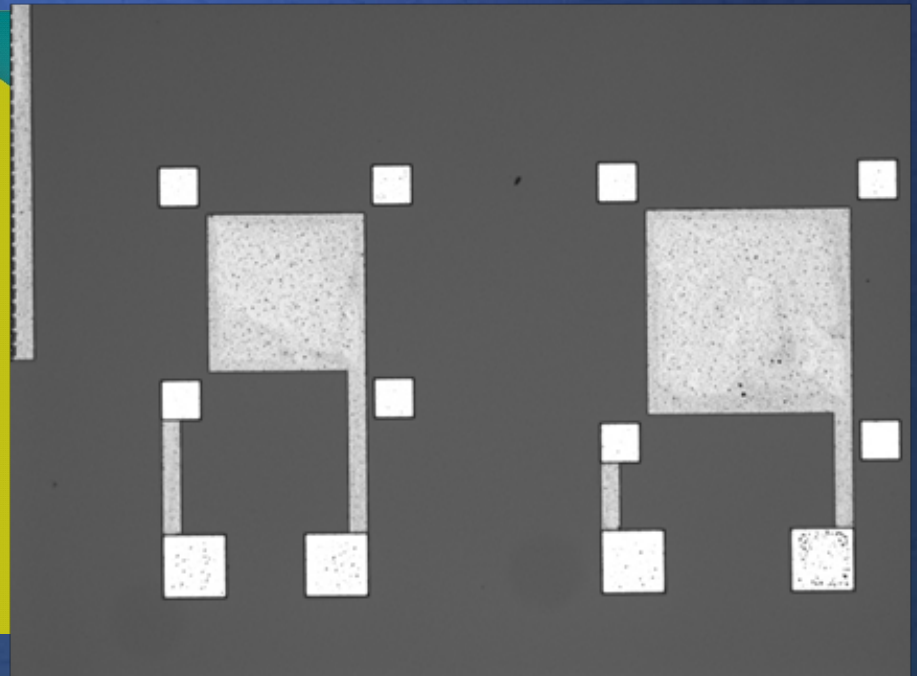
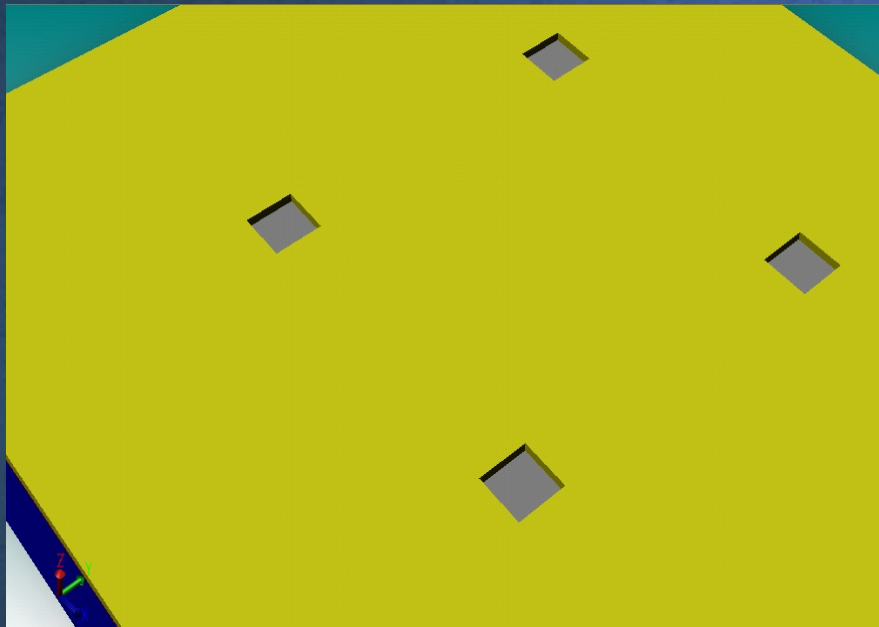
Accelerometer Fabrication

- Si/ Si₃N₄/ PI 5878G/ Si₃N₄/ Al.
- Metallization layer fabrication.



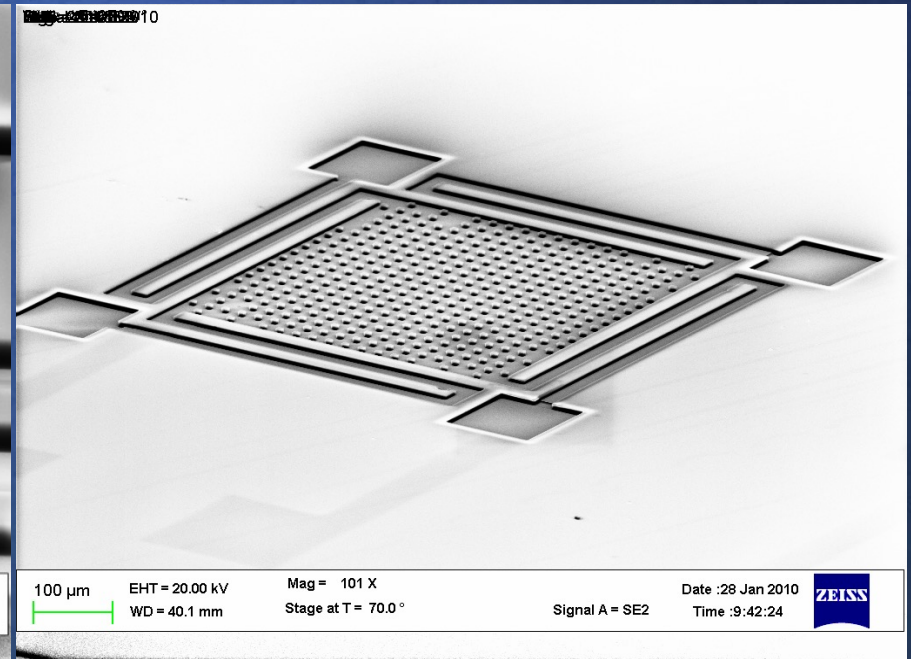
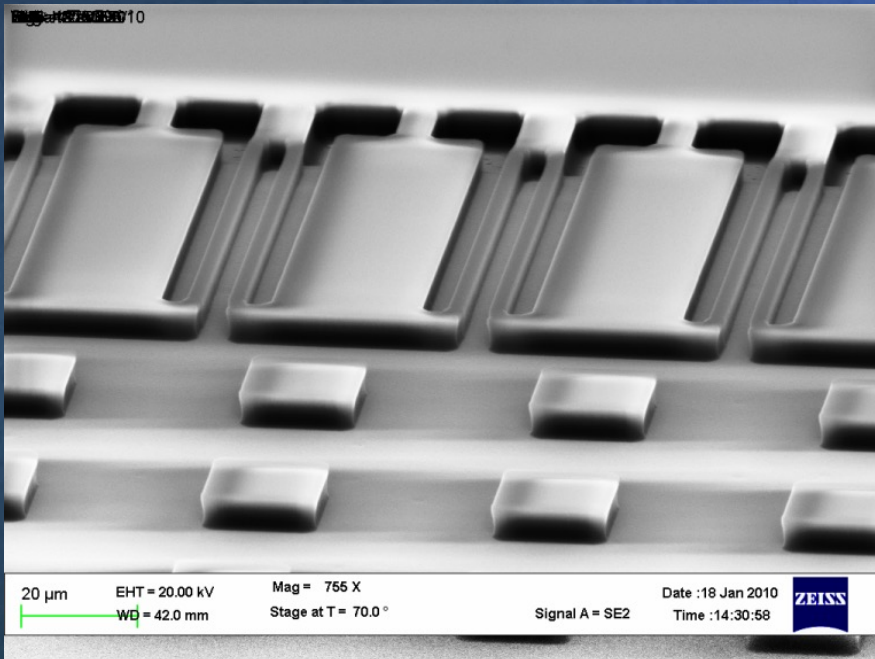
Accelerometer Fabrication

- Polyimide as sacrificial layer and patterning.
- Curing to obtain thickness of $\sim 2.0 \mu\text{m}$



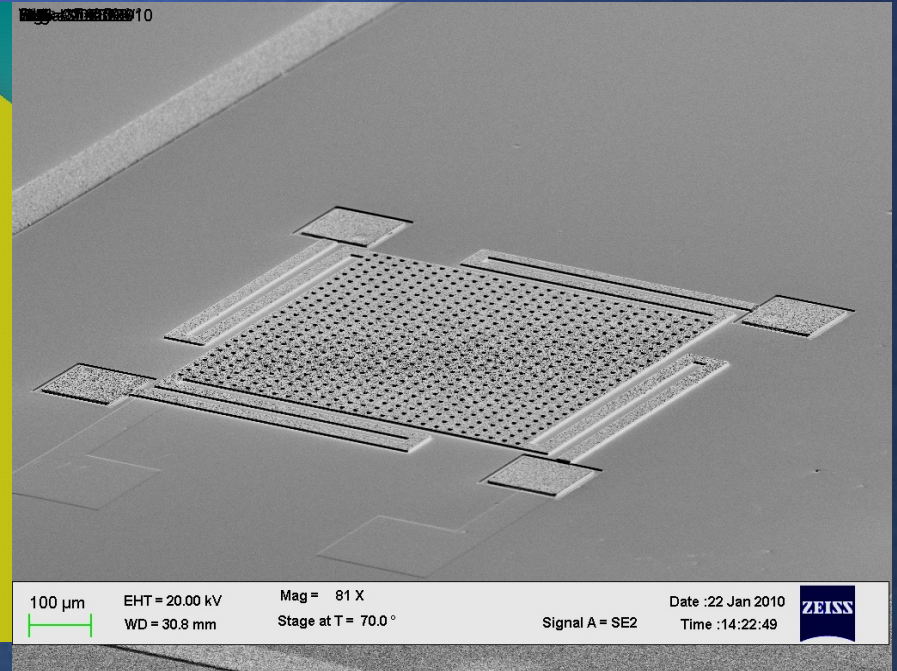
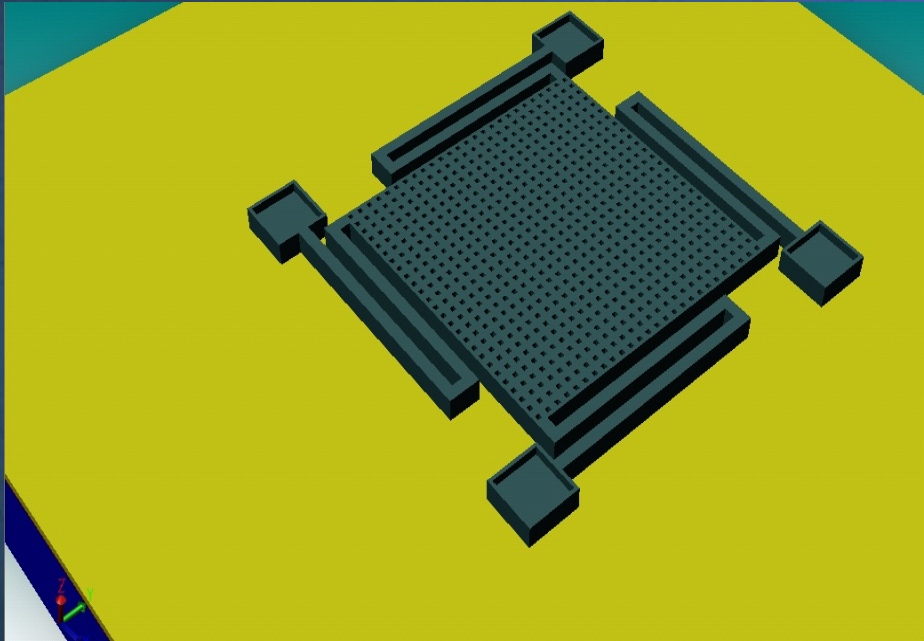
Accelerometer Fabrication

- Gold seed layer for electroplating ($\sim 0.1 \mu\text{m}$).
- Mold photoresist ($\sim 6.0 \mu\text{m}$)



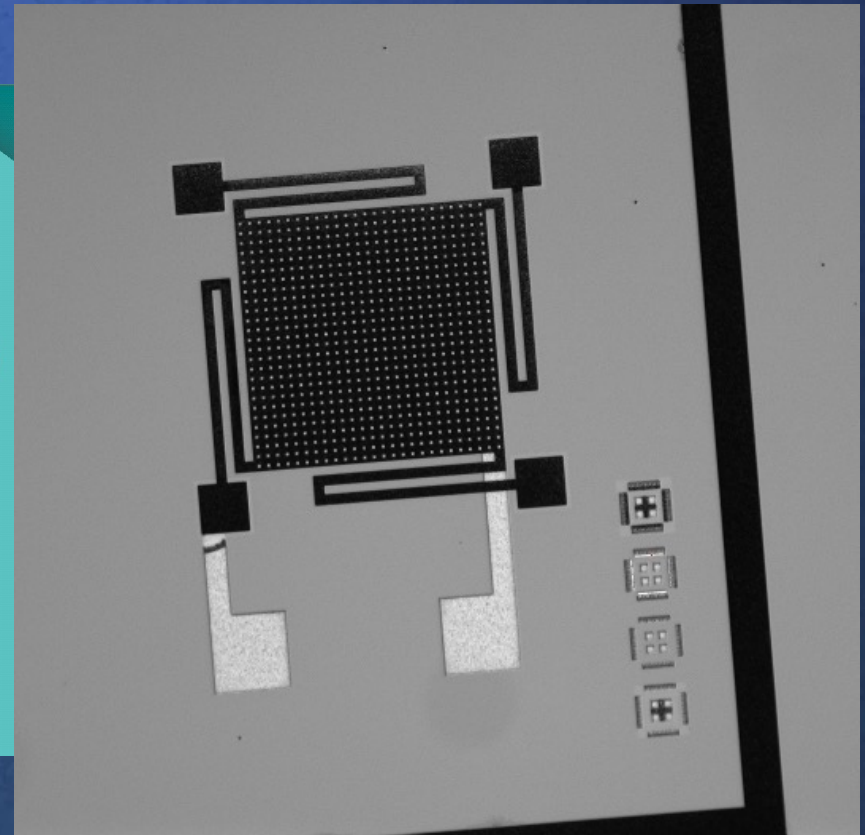
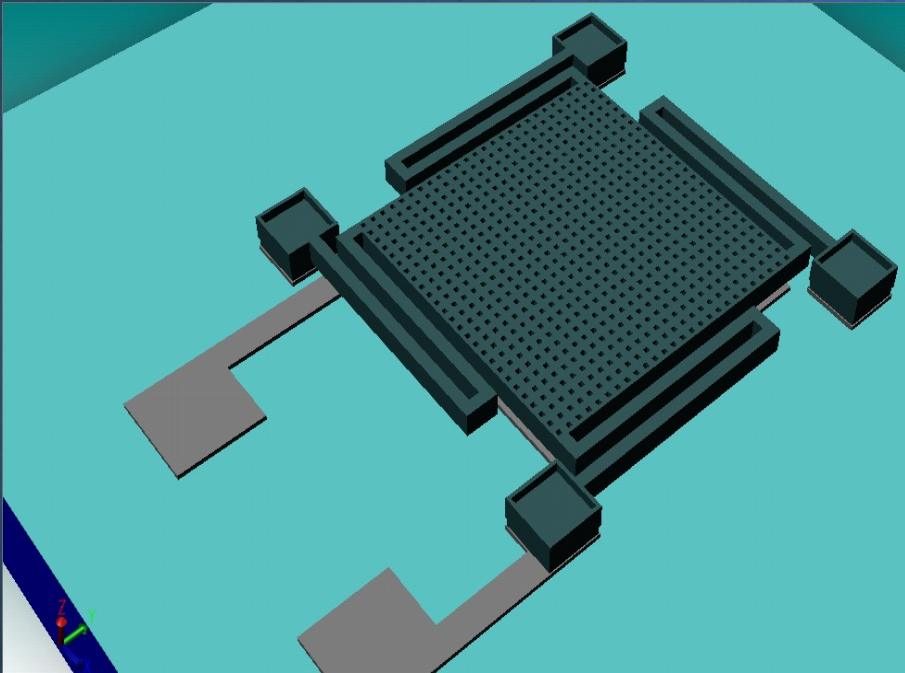
Accelerometer Fabrication

- UV-LIGA process to fabricate accelerometers.
- Ni electroplating to form the proof mass ($\sim 5.0 \mu\text{m}$).
- Resist removal and etching off of the gold seed layer.



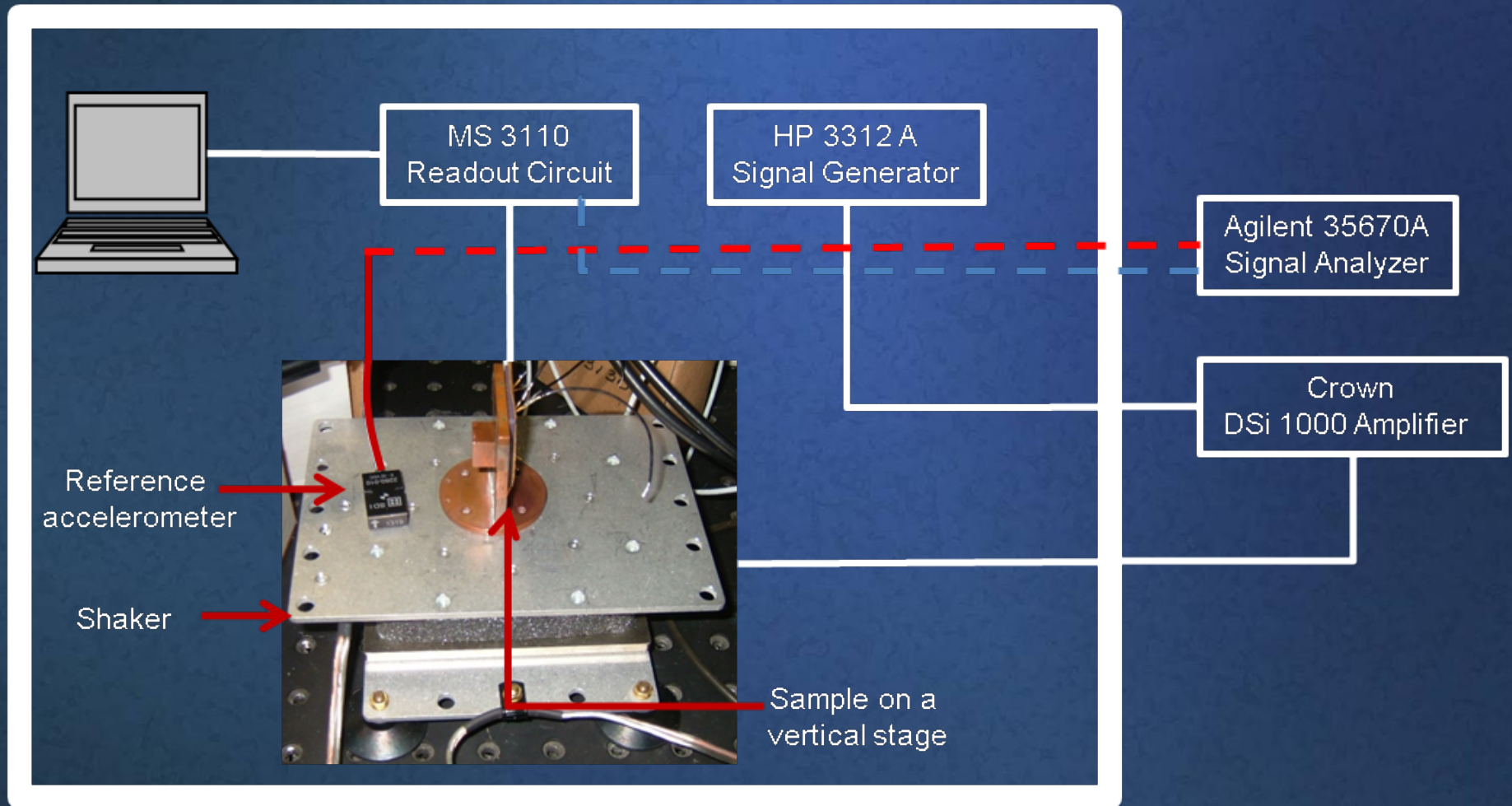
Accelerometer Fabrication

- Oxygen plasma ashing of the polyimide sacrificial layer to suspend the structure.



Setup for Characterization

Shielded room

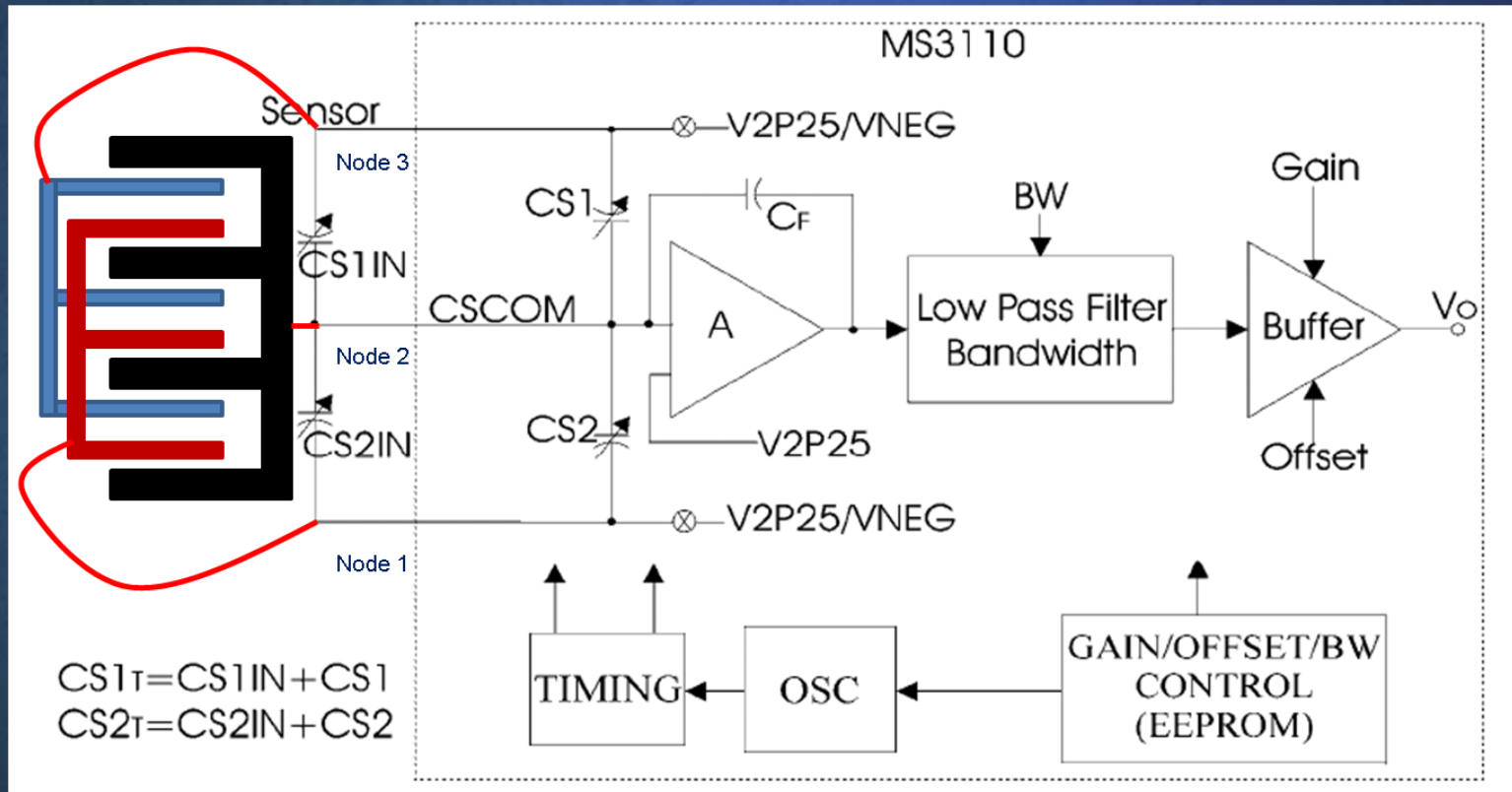


Setup for Characterization

CF (Trim capacitor)=5.130 pF
 CS1 and CS2=Variable capacitors
 Gain= 2 V/V
 $V_{ref} = 0.5 \text{ V}$

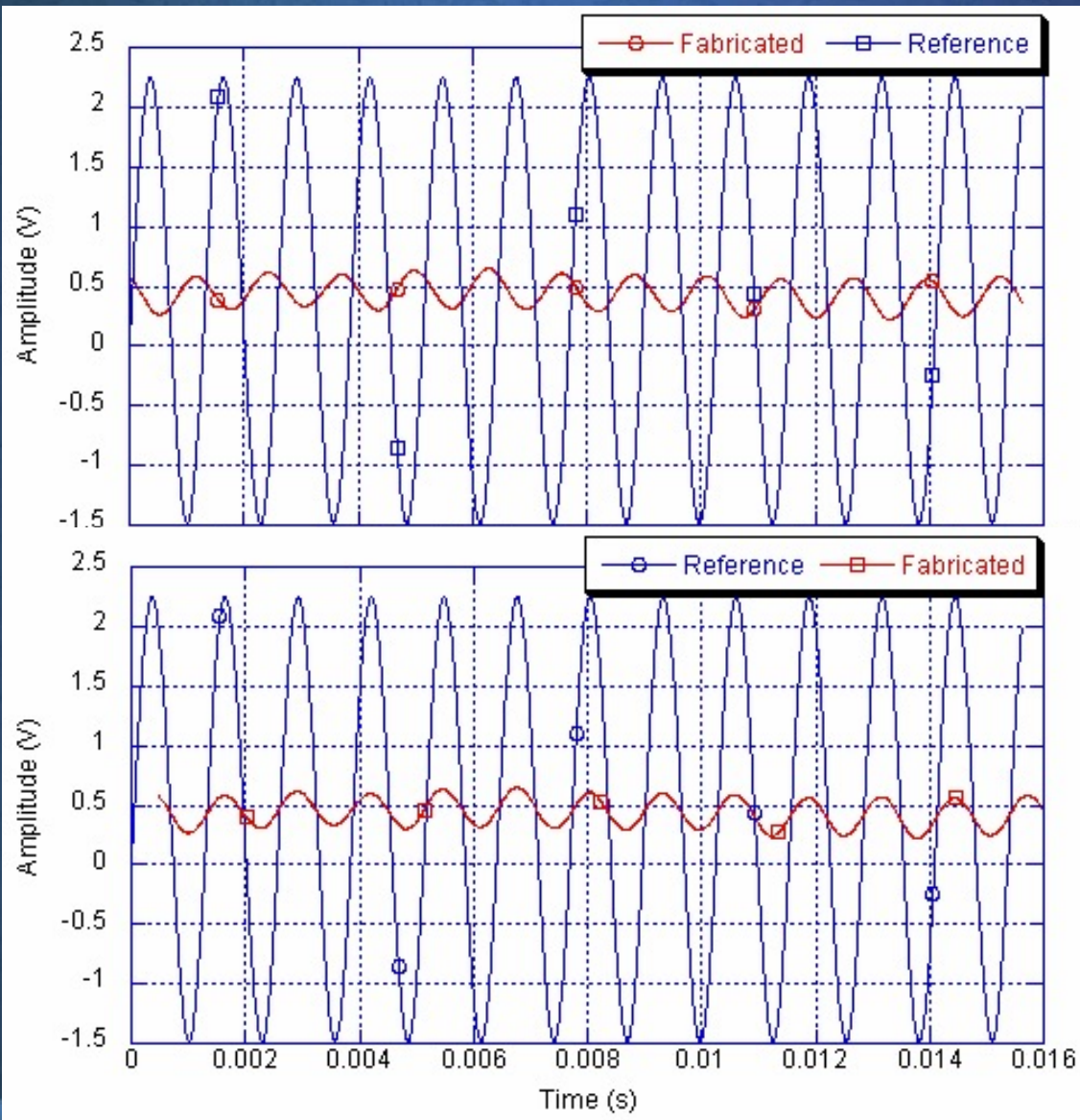
CS1IN and CS2IN: Device capacitances

$$V_{out} = 1.14 * V_{2P25} * Gain * \frac{CS2_T - CS1_T}{CF} + V_{ref}$$



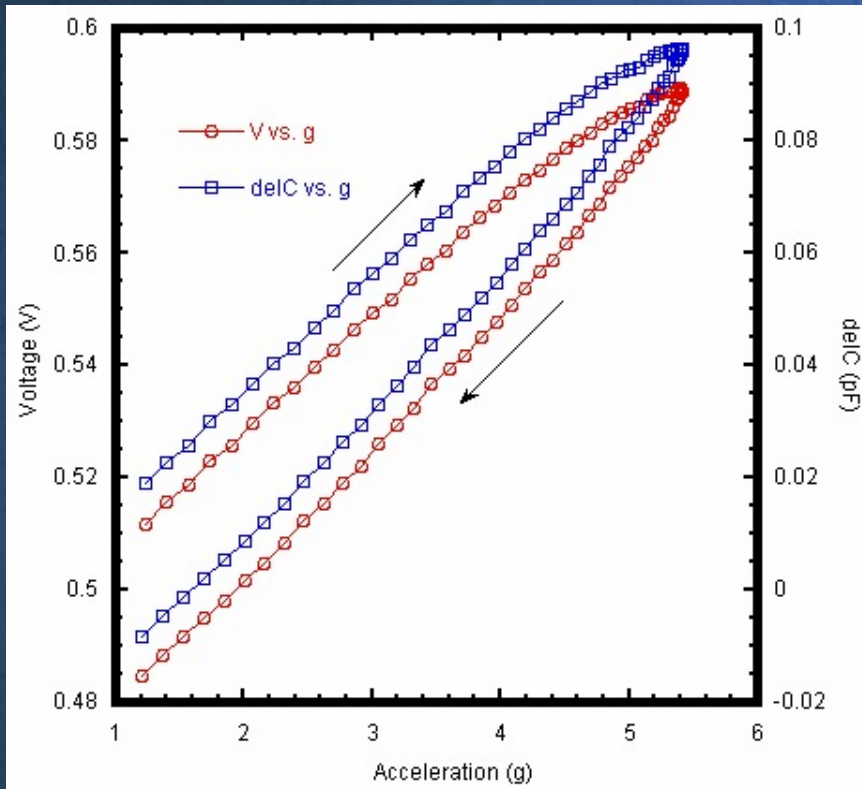
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Measurement Results

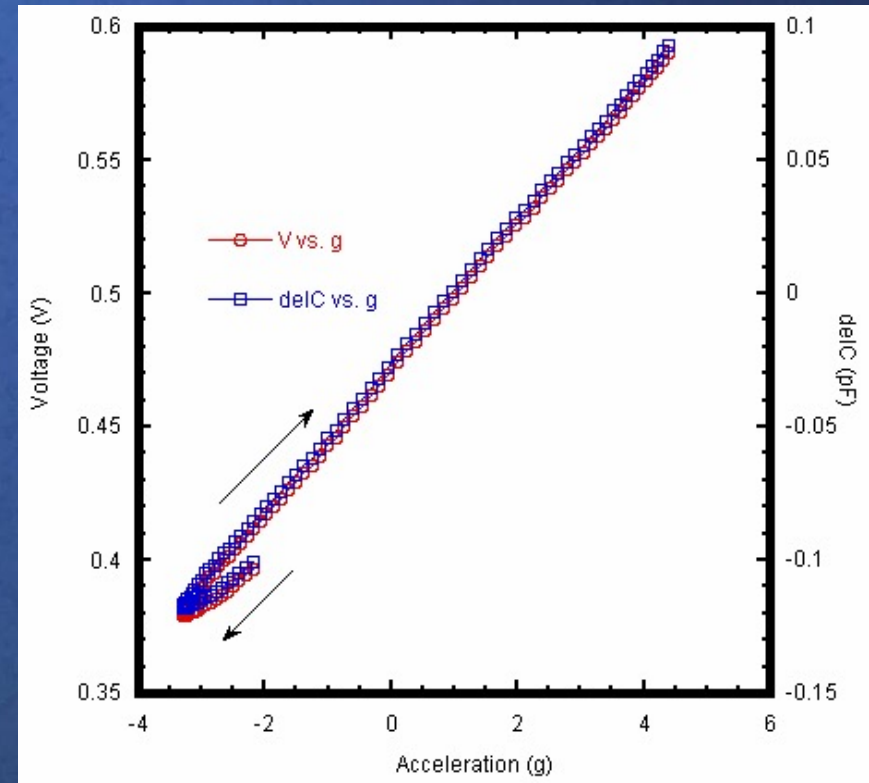


Measurement Results

- Voltage response and change in capacitance with respect to acceleration for z-axis accelerometers on Si and flexible substrate. Both samples are Device 2



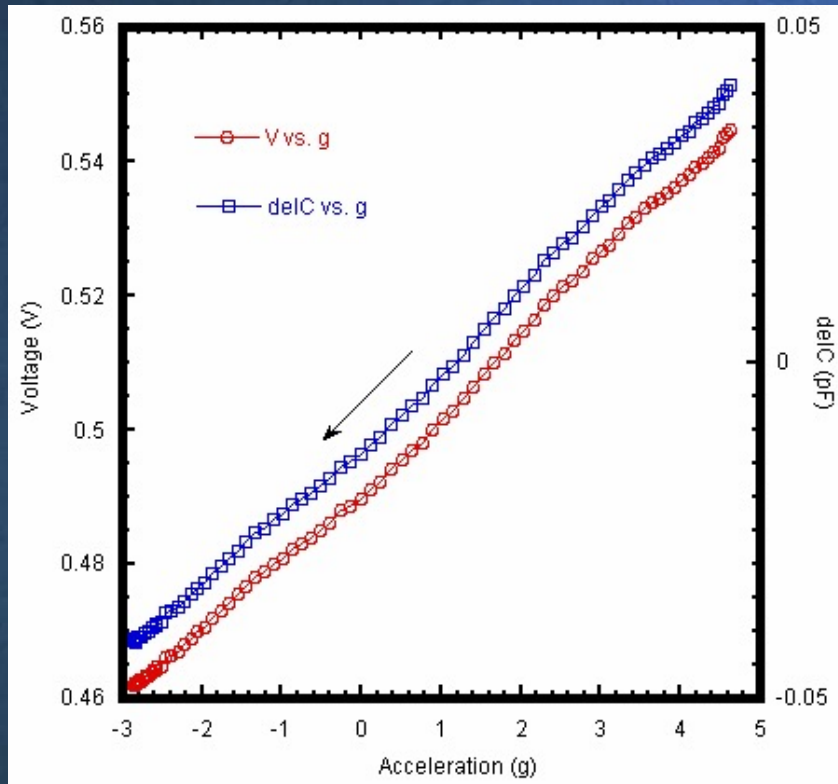
Si substrate, $\Delta C=21.9$ fF/g



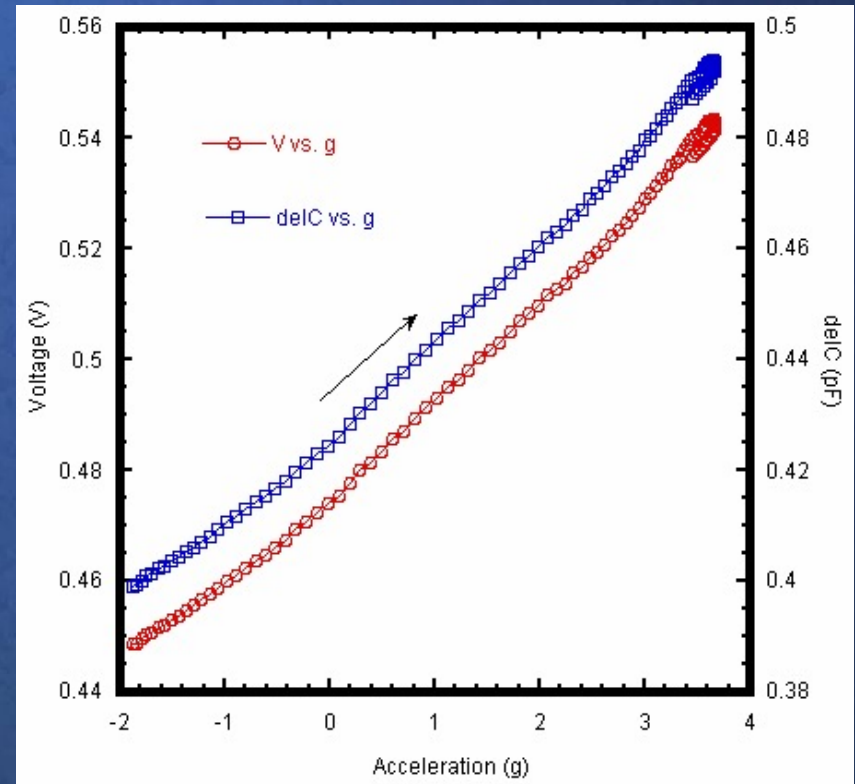
Flexible substrate, $\Delta C=27.7$ fF/g

Measurement Results

- Voltage response and change in capacitance with respect to acceleration for z-axis accelerometers on Si and flexible substrate. Both samples are Device 4b



Si substrate, $\Delta C=11$ fF/g



Flexible substrate, $\Delta C=17.5$ fF/g